



SKILL 18: Solving Equations with Rational Numbers

You can use the same procedures to solve equations with rational numbers that you used to solve equations with integers. You “undo” operations so that the variable is alone on one side of the equation.

Example 1

Solve: $\frac{2}{3}x = -\frac{1}{4}$.

$$\frac{2}{3}x = \frac{-1}{4}$$

Rewrite $-\frac{1}{4}$ as $\frac{-1}{4}$.

$$\frac{2}{3}x \div \frac{2}{3} = \frac{-1}{4} \div \frac{2}{3}$$

Undo multiplication by division. Divide both sides by $\frac{2}{3}$.

$$x = \frac{-1}{4} \cdot \frac{3}{2}$$

Change division by a fraction to multiplication by its reciprocal.

$$= \frac{-1 \cdot 3}{4 \cdot 2}$$

Multiply numerators. Multiply denominators.

$$x = \frac{-3}{8}$$

The solution is $-\frac{3}{8}$.

Example 2

Solve: $\frac{x}{-0.4} = 6$.

$$\frac{x}{-0.4} = 6$$

x is divided by -0.4 .

$$\frac{x}{-0.4} \cdot (-0.4) = 6 \cdot (-0.4)$$

Undo division by multiplication. Multiply both sides by -0.4 .

$$x = -2.4$$

The solution is -2.4 .

Guided Practice

Solve each equation. Check your solution.

1. $m - 5 = -\frac{1}{2}$

5 is _____ from m .
(added/subtracted)

Undo this operation by _____.
(addition/subtraction)

$$m - 5 + \underline{\hspace{2cm}} = -\frac{1}{2} + \underline{\hspace{2cm}}$$

$$x = \underline{\hspace{2cm}}$$

2. $-0.6x = -6$

x is multiplied by _____.

Undo multiplication by _____.

$$\frac{-0.6x}{-0.6} = \frac{-6}{-0.6}$$

$$x = \underline{\hspace{2cm}}$$

SKILL 18: Practice

Solve each equation. Check your solution.

1. $x + \frac{5}{7} = \frac{6}{7}$

$x = \underline{\hspace{2cm}}$

4. $k + 4\frac{1}{2} = 3\frac{1}{2}$

$k = \underline{\hspace{2cm}}$

7. $-3y = \frac{5}{8}$

$y = \underline{\hspace{2cm}}$

10. $t + \left(-1\frac{1}{2}\right) = -6\frac{1}{2}$

$t = \underline{\hspace{2cm}}$

13. $x - 3.2 = -20.8$

$x = \underline{\hspace{2cm}}$

16. $-\frac{4}{5}m = 6$

$m = \underline{\hspace{2cm}}$

19. $-\frac{1}{4}j = \frac{2}{3}$

$j = \underline{\hspace{2cm}}$

2. $x - \frac{1}{8} = -\frac{5}{8}$

$x = \underline{\hspace{2cm}}$

5. $\frac{n}{-4} = \frac{1}{2}$

$n = \underline{\hspace{2cm}}$

8. $10x = -7$

$x = \underline{\hspace{2cm}}$

11. $j - \left(-4\frac{1}{3}\right) = -10$

$j = \underline{\hspace{2cm}}$

14. $-0.25x = 2$

$x = \underline{\hspace{2cm}}$

17. $\frac{8}{9}t = -\frac{1}{3}$

$t = \underline{\hspace{2cm}}$

20. $-0.01k = 0.8$

$k = \underline{\hspace{2cm}}$

3. $6m = -\frac{1}{2}$

$m = \underline{\hspace{2cm}}$

6. $y - \frac{5}{8} = -\frac{3}{8}$

$y = \underline{\hspace{2cm}}$

9. $m + 9 = -11$

$m = \underline{\hspace{2cm}}$

12. $2k = \frac{1}{8}$

$k = \underline{\hspace{2cm}}$

15. $\frac{5}{16}n = -10$

$n = \underline{\hspace{2cm}}$

18. $y + 1\frac{1}{4} = 7\frac{1}{4}$

$y = \underline{\hspace{2cm}}$

21. $-6t = 6.6$

$t = \underline{\hspace{2cm}}$

Solve.

22. The price of a share of stock changed by $-\$19.20$ over a 5-day period. What was the average daily change in the price of a share of the stock? _____23. Janice plans to save $\$22.50$ each week until she has enough money to buy a $\$180$ bicycle. After how many weeks will she have enough money for the bicycle? _____**WEST PREP**

24. Solve $2x = -8.4$.

A -16.8

C 4.2

B -4.2

D -42

Skill 18

25. Multiply: $-\frac{3}{4} \cdot \left(-\frac{2}{3}\right)$.

F $\frac{1}{2}$

H $-\frac{1}{2}$

G $-\frac{5}{12}$

J $\frac{1}{8}$

Skill 17