Applications

1. For a fundraiser, students sell calendars and posters.

a. What equation shows how the income I for the fundraiser depends on the number of calendars c and the number of posters p that are sold?

b. What is the income if students sell 25 calendars and 18 posters?

c. What is the income if students sell 12 calendars and 15 posters?

d. What is the income if students sell 20 calendars and 12 posters?

e. Find three combinations of calendar sales and poster sales that will give an income of exactly $100.

f. Each answer in part (e) can be written as an ordered pair (c, p). Plot the ordered pairs on a coordinate grid.

g. Use your graph to estimate three other (c, p) pairs that would meet the $100 goal.

2. Kateri saves her quarters and dimes. She plans to exchange the coins for paper money when the total value equals $10.

a. How many coins does she need to make $10 if all the coins are quarters? If all the coins are dimes?

b. What equation relates the number of quarters x and the number of dimes y to the goal of $10?

c. Use the answers from part (a) to help you draw a graph showing all solutions to the equation.

d. Use the graph to find five combinations of dimes and quarters that will allow Kateri to reach her goal.

3. Students in Eric's gym class must cover a distance of 1,600 meters by running or walking. Most students run part of the way and walk part of the way. Eric can run at an average speed of 200 meters per minute and walk at an average speed of 80 meters per minute.

a. Suppose Eric runs for 4 minutes and walks for 8 minutes. How close is he to the 1,600-meter goal?

b. Write an equation for the distance d Eric will cover if he runs for x minutes and walks for y minutes.

c. Find three combinations of running and walking times for which Eric would cover 1,600 meters.

d. Plot the ordered pairs from part (c) on a graph. Use the graph to estimate several other combinations of running and walking times for which Eric would cover 1,600 meters.

4. Kevin said that if you triple his age, the result will be 1 less than his mother's age.

a. Which, if any, of these equations shows the relationship between Kevin's age x and his mother's age y? Choose all that are correct.

$3x - y = 1$ $\quad y - 3x = 1$ $\quad 3x + 1 = y$ $\quad 3x = 1 - y$

b. Find three pairs of values (x, y) that satisfy the equation relating Kevin's age and his mother's age. Plot these ordered pairs, and draw the line through the points.

c. Use the graph to estimate three other ordered pairs that satisfy the equation. Use the equation to check the estimates.

Find three pairs of values (x, y) that satisfy each equation. Plot those points and use the pattern to find two more solution pairs. (Hint: What is y if $x = 0$? What is x if $y = 0$?)

5. $6 = 3x - 2y$

6. $10 = x + 2y$

7. $2x + y = 6$

8. $-3x + 4y = -4$

Write the equation in equivalent $Ax + By = C$ form. Then, identify the x-intercept, y-intercept, and slope.

9. $y = 4x - 2$

10. $y = -3x + 5$

11. $y = x - 7$

12. $y = 5x + 3$

13. $y = -8x - 12$

14. $y = -9x + 5$

For Exercises 15–20, write the equation in $y = mx + b$ form. Identify the x-intercept, y-intercept, and slope.

15. $-2x - y = -5$

16. $6x + 3y = -9$

17. $x - y = 4$

18. $3x + 4y = 12$

19. $-7x + 2y = -16$

20. $x - 5y = 55$

21. Look back over your work for Exercises 9–20. Look for patterns relating the standard form of the equation, $Ax + By = C$, to the x-intercept, y-intercept, and slope.

a. Write a general formula for calculating the x-intercept from the values of A, B, and C.

b. Write a general formula for calculating the y-intercept from the values of A, B, and C.

c. Write a general formula for calculating the slope from the values of A, B, and C.

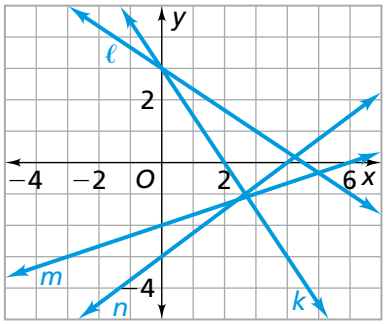
22. Tell which line below is the graph of each equation in parts (a)–(d). Explain.

a. $2x + 3y = 9$

b. $3x - 4y = 12$

c. $x - 3y = 6$

d. $3x + 2y = 6$



23. In Exercise 1, suppose the goal is to raise \$600. One equation relating the calendar and poster sales to the \$600 goal is $3c + 2p = 600$. Suppose the company donating the calendars and posters said they would provide a total of 250 items.

a. What equation relates c and p to the 250 items donated?

b. Graph both equations on the same grid. Find the coordinates of the intersection point. Explain what these coordinates tell you about the fundraising situation.

24. In Exercise 2, one equation relating Kateri's quarters and dimes to her goal of \$10 (1,000 cents) is $25x + 10y = 1{,}000$. Suppose Kateri collects 70 coins to reach her goal.

a. What equation relates x and y to the number of coins Kateri collected?

b. Graph both equations on the same grid. Find the coordinates of the intersection point. Explain what these coordinates tell you about this situation.

25. In Exercise 3, one equation relating the times Eric spends running and walking to reach the goal of covering 1,600 meters is $200x + 80y = 1{,}600$. Suppose Eric runs and walks for a total of 12 minutes to reach his goal.

a. What equation relates x and y to Eric's total time?

b. Graph both equations on the same grid. Find the coordinates of the intersection point. Explain what these coordinates tell you about this situation.

26. In Exercise 4, one equation relating the ages of Kevin and his mother is $y - 3x = 1$. The sum of Kevin's age and his mother's age is 61 years.

a. What equation relates Kevin's and his mother's ages to the total of their ages?

b. Graph both equations on the same grid. Find the coordinates of the intersection point. Explain what these coordinates tell you about the ages of Kevin and his mother.

27. Use graphing methods to solve each system of equations. (**Hint:** If you are using a graphing calculator, you can determine a good graphing window by first finding the x- and y-intercepts of each graph.)

a. $x - y = -4$ and $x + y = 6$

b. $-2x + y = 3$ and $x + 2y = -9$

c. $-2x + y = 1$ and $4x - 2y = 6$

Connections

For Exercises 28–33, solve the inequality. Then, write the solution using symbols, write the solution using words, and graph the solution on a number line.

28. $x + 3 < 5$

29. $x - 12 > -4$

30. $14 + x \leq -2$

31. $2x + 7 \geq -3$

32. $7x + 3 \leq -17 + 2x$

33. $-3 - 4x \geq 5x + 24$

34. The cost C to make T-shirts for a softball team is represented by the equation $C = 24 + 6N$, where N represents the number of T-shirts.

a. Find the coordinates of a point that lies on the graph of this equation. Explain what the coordinates mean in this context.

b. Find the coordinates of a point above the line. Explain what the coordinates mean in this context.

c. Find the coordinates of a point below the line. Explain what the coordinates mean in this context.

35. **a.** Which of the following points lies on the line $y = 4x - 3$? Describe where the other three points are located in relation to the line.

$(2, 1)$ $(2, 2)$ $(2, 5)$ $(2, 8)$

b. Find another point that lies on the line $y = 4x - 3$. Find three more points that lie above the line.

c. The points $(-2, -11)$ and $(3, 9)$ lie on the graph of $y = 4x - 3$. Use this information to find two points that make the inequality $y < 4x - 3$ true, and two points that make the inequality $y > 4x - 3$ true.

Write an equation of a line parallel to the given line.

36. $y = 4x + 6$

37. $-6x + y = 3$

38. $x + y = 9$

39. $x + 4y = -20$

40. $y = -\frac{3}{4}x - 2$

41. $7x + y = -12$

For Exercises 42–47, write an equation of a line perpendicular to the given line.

42. $y = -4x + 2$

43. $y = -\frac{2}{3}x - 7$

44. $y = 6x + 12$

45. $-2x + y = -1$

46. $x - 4y = 20$

47. $2x + 3y = 8$

48. Tell whether each ordered pair is a solution of $3x - 5y = 15$. Show how you know.

a. $(-2, -4)$

b. $(0, -3)$

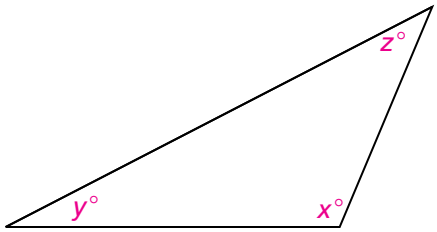
c. $(-10, 9)$

d. $(-5, -6)$

e. $(-10, -9)$

f. $(-4, -5.4)$

49. The angle measures of the triangle are $x°$, $y°$, and $z°$.



a. What equation shows how z depends on x and y?

b. Find five combinations of values for x and y for which the value of z is 40.

50. Multiple Choice Suppose k, m, and n are numbers and $k = m + n$. Which of the following statements must be true?

A. $k - m = n$

B. $m - k = n$

C. $2k = 2m + n$

D. $-n = k + m$

51. Multiple Choice Which equation is equivalent to $3x + 5y = 15$?

F. $3x = 5y + 15$

G. $x = -5y + 5$

H. $y = 0.6x + 3$

J. $y = -0.6x + 3$

52. Suppose you are given the linear equation $Ax + By = C$.

a. What is the slope of every line parallel to this line?

b. What is the slope of every line perpendicular to this line?

53. You will need two sheets of grid paper and two different cans with paper labels (for example, clam chowder and stewed tomatoes cans). On grid paper, trace the top and bottom of each can. Cut these out. Now carefully remove the labels and trace these on grid paper.

a. Estimate and compare the surface areas of the cans. (**Hint:** The surface area of a can = label + top + bottom or S.A. $= \ell w + 2\pi r^2$.)

b. After Joel removes his two labels, he notices that the labels are the exact same size and shape. Explain how this can happen.

54. Multiple Choice Which values are solutions of the quadratic equation $x^2 + 8x - 33 = 0$?

A. $x = -11$ and $x = -3$

B. $x = 11$ and $x = -3$

C. $x = -11$ and $x = 3$

D. $x = 11$ and $x = 3$

55. Use the graph of $y = x^2 + 8x - 33$ to find the solution of each inequality.

a. $x^2 + 8x - 33 > 0$

b. $x^2 + 8x - 33 < 0$

56. Tell whether each line has a slope of $-\frac{1}{2}$.

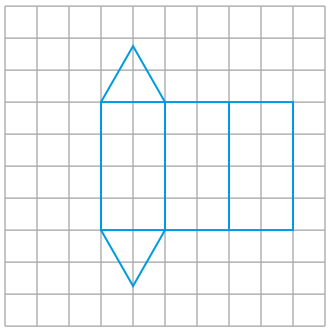
a. $y = \frac{-1}{-2}x + 3$

b. $y = \frac{-1}{2}x + 3$

c. $y = \frac{1}{-2}x + 3$

d. $y = -\frac{1}{2}x + 3$

57. a. What shape will this net make if it is cut out and folded?



b. Find the surface area of the shape.

c. Find the volume of the shape.

Without graphing, decide whether the lines are *parallel*, *perpendicular*, or *neither*.

58. $3x + 6y = 12$ and $y = 10 + \frac{-1}{2}x$

59. $y = -x + 5$ and $y = x + 5$

60. $y = 2 - 5x$ and $y = -5x + 2$

61. $y = -3 + 5x$ and $y = \frac{-x}{5} + 3$

62. $10x + 5y = 20$ and $y = 10x + 20$

Extensions

63. Jasmine wants to run a marathon. She knows she will have to walk some of the 26.2 miles, but she wants to finish in 5 hours. She plans to run 10-minute miles and walk 15-minute miles. Let x represent the number of minutes Jasmine runs. Let y represent the number of minutes she walks.

a. What equation relates x and y to the goal of completing the race in 5 hours?

b. What equation relates x and y to the goal of covering 26.2 miles?

c. For each equation, find several ordered-pair solutions (x, y). Then, plot the points with those coordinates and use the pattern to draw a graph of the equation. Graph both equations on the same grid.

d. Use the graphs to estimate the combination of running and walking times that will allow Jasmine to complete the marathon in exactly 5 hours.

64. In Exercise 63, suppose Jasmine decides she wants to finish the marathon in less than 5 hours.

a. Find five combinations of running and walking times that give a total time of less than 5 hours.

b. Express the condition that the total running and walking times must be less than 5 hours as an inequality.

c. Make a graph of all the solutions of the inequality.

d. Graph the linear equation from Exercise 63, part (b) on the same grid as the inequality. Explain how the result shows Jasmine's options for running and walking times if she wants to finish the marathon in 5 hours or less.