

Elimination Practice

$$\begin{array}{r}
 1. \ x - y = 1 \\
 + \ x + y = -9 \\
 \hline
 2x = -8 \\
 \frac{2x}{2} = \frac{-8}{2} \\
 x = -4
 \end{array}$$

$$\begin{array}{r}
 x + y = -9 \\
 -4 + y = -9 \\
 +4 \quad +4 \\
 \hline
 y = -5
 \end{array}$$

$(-4, -5)$

$$\begin{array}{r}
 2. \ p + q = -2 \\
 + \ p - q = 8 \\
 \hline
 2p = 6 \\
 \frac{2p}{2} = \frac{6}{2} \\
 p = 3
 \end{array}$$

$$\begin{array}{r}
 p + q = -2 \\
 3 + q = -2 \\
 -3 \quad -3 \\
 \hline
 q = -5
 \end{array}$$

$(3, -5)$

$$\begin{array}{r}
 3. \ 4x + y = 23 \\
 + \ 3x - y = 12 \\
 \hline
 7x = 35 \\
 \frac{7x}{7} = \frac{35}{7} \\
 x = 5
 \end{array}$$

$$\begin{array}{r}
 4x + y = 23 \\
 4(5) + y = 23 \\
 20 + y = 23 \\
 -20 \quad -20 \\
 \hline
 y = 3
 \end{array}$$

$(5, 3)$

$$\begin{array}{r}
 4. \ 2x + 5y = -3 \\
 - \ 2x + 2y = 6 \\
 \hline
 3y = -9 \\
 \frac{3y}{3} = \frac{-9}{3} \\
 y = -3
 \end{array}$$

$$\begin{array}{r}
 2x + 5y = -3 \\
 2x + 5(-3) = -3 \\
 2x - 15 = -3 \\
 +15 \quad +15 \\
 \hline
 2x = 12 \\
 \frac{2x}{2} = \frac{12}{2} \\
 x = 6
 \end{array}$$

$(6, -3)$

$$\begin{array}{r}
 5. \ 3x + 2y = -1 \\
 - \ 4x + 2y = -6 \\
 \hline
 -x = 5 \\
 \frac{-x}{-1} = \frac{5}{-1} \\
 x = -5
 \end{array}$$

$$\begin{array}{r}
 3x + 2y = -1 \\
 3(-5) + 2y = -1 \\
 -15 + 2y = -1 \\
 +15 \quad +15 \\
 \hline
 2y = 14 \\
 \frac{2y}{2} = \frac{14}{2} \\
 y = 7
 \end{array}$$

$(-5, 7)$

$$\begin{array}{r}
 6. \ 5x + 3y = 22 \\
 - \ 5x - 2y = 2 \\
 \hline
 5y = 20 \\
 \frac{5y}{5} = \frac{20}{5} \\
 y = 4
 \end{array}$$

$$\begin{array}{r}
 5x + 3y = 22 \\
 5x + 3(4) = 22 \\
 5x + 12 = 22 \\
 -12 \quad -12 \\
 \hline
 5x = 10 \\
 \frac{5x}{5} = \frac{10}{5} \\
 x = 2
 \end{array}$$

$(2, 4)$

$$\begin{array}{r} 7. \quad 5x + 2y = 7 \\ - \quad -2x + 2y = -14 \end{array}$$

$$\frac{7x}{7} = \frac{21}{7}$$

$$x = 3$$

$$5(3) + 2y = 7$$

$$\begin{array}{r} 15 + 2y = 7 \\ -15 \quad -15 \end{array}$$

$$\frac{2y}{2} = \frac{-8}{2}$$

$$y = -4$$

$$(3, -4)$$

$$\begin{array}{r} 8. \quad 3x - 9y = -12 \\ - \quad 3x - 15y = -6 \end{array}$$

$$\frac{6y}{6} = \frac{-6}{6}$$

$$y = -1$$

$$3x - 9(-1) = -12$$

$$\begin{array}{r} 3x + 9 = -12 \\ -9 \quad -9 \end{array}$$

$$\frac{3x}{3} = \frac{-21}{3}$$

$$x = -7$$

$$(-7, -1)$$

$$\begin{array}{r} 9. \quad -4c - 2d = -2 \\ - \quad 2c - 2d = -14 \end{array}$$

$$\frac{-6c}{-6} = \frac{12}{-6}$$

$$c = -2$$

$$-4c - 2d = -2$$

$$-4(-2) - 2d = -2$$

$$8 - 2d = -2$$

$$\begin{array}{r} -8 \quad -8 \end{array}$$

$$\frac{-2d}{-2} = \frac{-10}{-2}$$

$$d = 5$$

$$(-2, 5)$$

$$\begin{array}{r} 10. \quad 2x - 6y = 6 \\ - \quad -2x + 3y = 24 \end{array}$$

$$\frac{-9y}{-9} = \frac{-18}{-9}$$

$$y = 2$$

$$2x - 6y = 6$$

$$2x - 6(2) = 6$$

$$2x - 12 = 6$$

$$\begin{array}{r} +12 \quad +12 \end{array}$$

$$\frac{2x}{2} = \frac{18}{2}$$

$$x = 9$$

$$(9, 2)$$

$$\begin{array}{r} 11. \quad 7x + 2y = 2 \\ - \quad 7x - 2y = -30 \end{array}$$

$$\frac{4y}{4} = \frac{32}{4}$$

$$y = 8$$

$$7x + 2(8) = 2$$

$$7x + 16 = 2$$

$$\begin{array}{r} -16 \quad -16 \end{array}$$

$$\frac{7x}{7} = \frac{-14}{7}$$

$$x = -2$$

$$(-2, 8)$$

$$\begin{array}{r} 12. \quad 4.25x - 1.28y = -9.2 \\ + \quad x + 1.28y = 17.6 \end{array}$$

$$\frac{5.25x}{5.25} = \frac{8.4}{5.25}$$

$$x = 1.6$$

$$4.25(1.6) - 1.28y = -9.2$$

$$6.8 - 1.28y = -9.2$$

$$\begin{array}{r} -6.8 \quad -6.8 \end{array}$$

$$\frac{-1.28y}{-1.28} = \frac{-16}{-1.28}$$

$$y = 12.5$$

$$(1.6, 12.5)$$

More Challenging

Use elimination to solve each system of equations.

1. $5[x + y = -9] \rightarrow 5x + 5y = -45$
 $5x - 2y = 32 \rightarrow -5x - 2y = 32$

$$\begin{array}{r} 5x + 5y = -45 \\ -5x - 2y = 32 \\ \hline 7y = -77 \\ \frac{7y}{7} = \frac{-77}{7} \\ y = -11 \end{array}$$

$$\begin{array}{r} x + y = -9 \\ x + (-11) = -9 \\ \hline +11 \quad +11 \\ \hline x = 2 \end{array}$$

(2, -11)

2. $3x + 2y = -9$
 $2[x - y = -13] \rightarrow 2x - 2y = -26$

$$\begin{array}{r} 3x + 2y = -9 \\ 2x - 2y = -26 \\ \hline 5x = -35 \\ \frac{5x}{5} = \frac{-35}{5} \\ x = -7 \end{array}$$

$$\begin{array}{r} x - y = -13 \\ -7 - y = -13 \\ \hline +7 \quad +7 \\ \hline -y = -6 \\ y = 6 \end{array}$$

(-7, 6)

3. $2x + 5y = 3$
 $2[-x + 3y = -7] \rightarrow -2x + 6y = -14$

$$\begin{array}{r} 2x + 5y = 3 \\ -2x + 6y = -14 \\ \hline 11y = -11 \\ \frac{11y}{11} = \frac{-11}{11} \\ y = -1 \end{array}$$

$$\begin{array}{r} -x + 3(-1) = -7 \\ -x - 3 = -7 \\ \hline +3 \quad +3 \\ \hline -x = -4 \\ \frac{-x}{-1} = \frac{-4}{-1} \\ x = 4 \end{array}$$

(4, -1)

4. $2[2x + y = 3] \rightarrow 4x + 2y = 6$
 $-4x - 4y = -8$

$$\begin{array}{r} 4x + 2y = 6 \\ -4x - 4y = -8 \\ \hline -2y = -2 \\ \frac{-2y}{-2} = \frac{-2}{-2} \\ y = 1 \end{array}$$

$$\begin{array}{r} 2x + (-1) = 3 \\ -1 - 1 \\ \hline 2x = 2 \\ \frac{2x}{2} = \frac{2}{2} \\ x = 1 \end{array}$$

(1, 1)

5. $4x - 2y = -14$
 $-2[3x - y = -8] \rightarrow -6x + 2y = 16$

$$\begin{array}{r} 4x - 2y = -14 \\ -6x + 2y = 16 \\ \hline -2x = 2 \\ \frac{-2x}{-2} = \frac{2}{-2} \\ x = -1 \end{array}$$

$$\begin{array}{r} 3(-1) - y = -8 \\ -3 - y = -8 \\ \hline +3 \quad +3 \\ \hline -y = -5 \\ \frac{-y}{-1} = \frac{-5}{-1} \\ y = 5 \end{array}$$

(-1, 5)

6. $3[2x + y = 0] \rightarrow 6x + 3y = 0$
 $5x + 3y = 2$

$$\begin{array}{r} 6x + 3y = 0 \\ -5x + 3y = 2 \\ \hline x = -2 \end{array}$$

$$\begin{array}{r} 2(-2) + y = 0 \\ -4 + y = 0 \\ \hline +4 \quad +4 \\ \hline y = 4 \end{array}$$

(-2, 4)

