

Warm Up

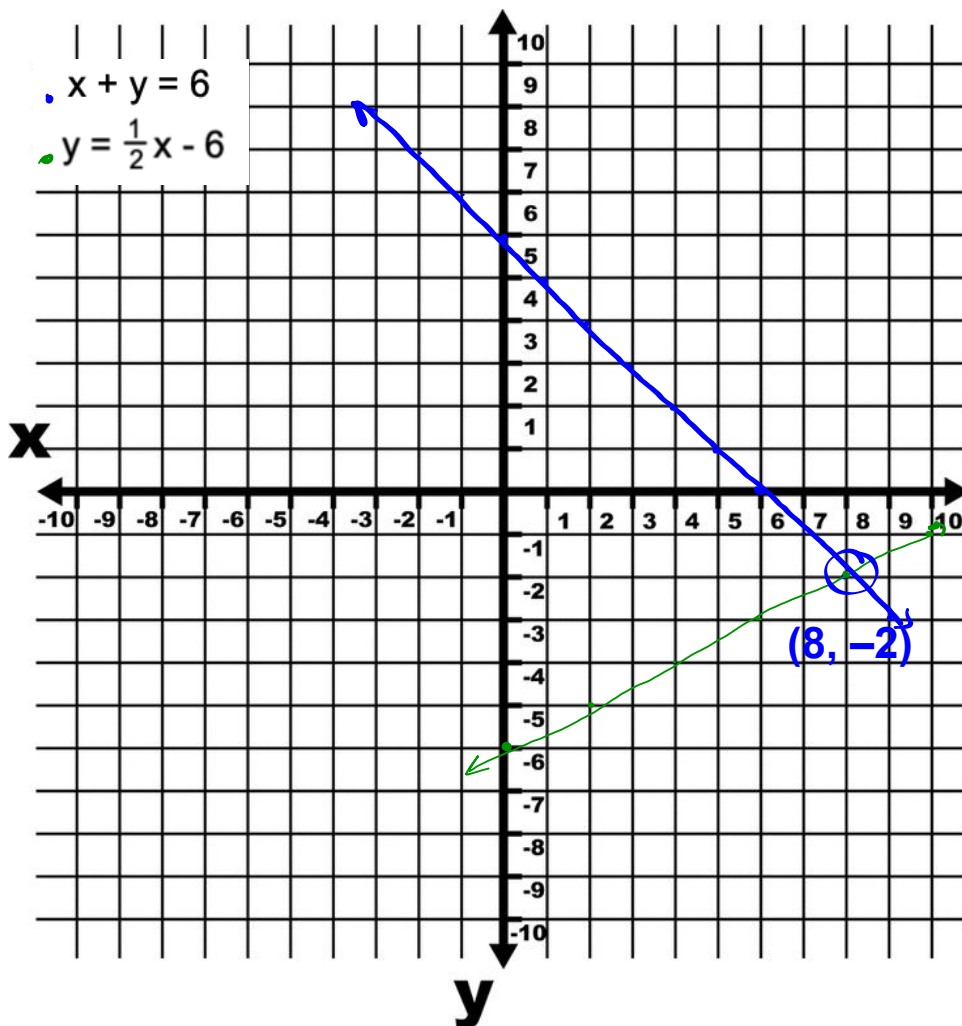
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Graph the following two equations on the same graph:

$$x + y = 6$$

$$y = \frac{1}{2}x - 6$$

Do they have a common solution?



Homework Questions?

For Exercises 9–14, write the equation in $y = mx + b$ form.

9. $4x + 6y + 12 = 0$

10. $-7x + 9y + 4 = 0$

11. $-4x - 2y - 6 = 0$

12. $-x + 4y = 0$

13. $2x - 2y + 2 = 0$

14. $25x + 5y - 15 = 0$

16. A seventh-grade class sells mouse pads and cell phone cases with their school logo on them. The class earns \$2 profit for each mouse pad sold and \$4 profit for each cell phone case sold. They sell 100 items in total for a profit of \$268.

- a. Write two equations that represent the relationship between the number of mouse pads sold m and the number of cell phone cases sold c .
- b. How many mouse pads and how many cell phone cases were sold?

Let $x =$ # mouse pads

Let $y =$ # cases =

$$\begin{cases} 2x + 4y = 268 \\ x + y = 100 \end{cases}$$

$$\frac{2x + 4y}{2} = \frac{268}{2}$$

$$x + 2y = 134$$

$$-2y \quad -2y$$

$$x = -2y + 134$$

$$\begin{array}{r} x + y = 100 \\ -y \quad -y \\ \hline x = -y + 100 \end{array}$$

$$\begin{array}{r} -y + 100 = -2y + 134 \\ -100 \quad -100 \\ \hline \end{array}$$

$$-y = -2y + 34$$

$$-34 \quad -34$$

$$-y - 34 = -2y$$

$$\begin{array}{r} +y \quad +y \\ \hline \end{array}$$

$$-34 = -y$$

$$-1 \quad -1$$

$$34 = y$$

Ways to solve systems of equations:

We currently have 2!

1. Graphing
2. Symbolically using
Equivalent Equations

$$x + y = 5$$

$$x = y + 7$$

already telling us what $x =$

we could

$$\begin{array}{r} x + y = 5 \\ - y - y \\ \hline x = 5 - y \end{array}$$

Equivalent Equations

$$\begin{cases} x = 5 - y \\ x = y + 7 \end{cases}$$

and then solve

$$\begin{array}{r} y + 7 = 5 - y \\ + y \\ \hline 2y + 7 = 5 \\ - 7 - 7 \\ \hline 2y = -2 \\ \frac{2y}{2} = \frac{-2}{2} \\ y = -1 \end{array}$$

OR, since we know that $x = y + 7$ we can substitute $y + 7$ in for the value of x in the first equation.

$$\begin{cases} x + y = 5 \\ x = y + 7 \end{cases}$$

$$\begin{array}{r} x + y = 5 \\ (y + 7) + y = 5 \\ 2y + 7 = 5 \\ - 7 - 7 \\ \hline 2y = -2 \\ \frac{2y}{2} = \frac{-2}{2} \\ y = -1 \end{array}$$

and then solve

$$\begin{array}{r} x + y = 5 \\ x - 1 = 5 \\ + 1 + 1 \\ \hline x = 6 \end{array}$$

$(6, -1)$

This is substitution!

Substitution

1. $y = 3 - 2x$
 $y = 2 - 3x$

$$3 - 2x = 2 - 3x$$

X- and Y-Intercepts

Solving Systems of Linear Equations by Substitution

$$\begin{aligned}
 4x + 4y &= 12 \\
 3x + y = 9 &\longrightarrow y = 9 - 3x \\
 4x + 4(9 - 3x) &= 12 \\
 4x + 36 - 12x &= 12 \\
 36 - 8x &= 12 \\
 -8x &= -24 \\
 x &= 3 \\
 \text{Solution } &(3, 0)
 \end{aligned}$$

Solve.

1. $y = 3 - 2x$
 $y = 2 - 3x$

2. $x + y = 5$
 $x = y + 7$

3. $x - y = 1 \rightarrow x = 1 + y$
 $2x + y = 8$
 $2(1 + y) + y = 8$

4. $3x - y = 9$
 $y = x + 5$

5. $3x + 4y = 26$
 $-2x + y = 1$

$2(1 + y) + y = 8$
 $2 + 2y + y = 8$

6. $y = 2x + 3$
 $y = 4x + 4$

7. $2x + 7y = 8$
 $x + 5y = 7$

$2 + 3y = 8$
 $\begin{array}{r} -2 \\ \hline 3y = 6 \\ \frac{3y}{3} = \frac{6}{3} \\ y = 2 \end{array}$

8. $y = 4x + 4$
 $y = 2x + 8$

9. $x + 3y = 17$
 $2x + 3y = 22$

10. $4x - 7y = 9$
 $y = x - 3$

Now solve for x.

Homework

Finish Problems 1-10